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(b. Shavli, Kovno [Kaunas] district [now Siauliai, Lithuania] S.S.R., 10 March 1869; d. Moscow, U.S.S.R., 8 May 1953)

mathematics.

The son of a clerk, Kagan entered Novorossysky University, Odessa, in 1887, but was expelled in 1889 for participating in the democratic students' movement and was sent to Ekaterinoslav (now Dnepropetrovsk). In 1892 he passed the examinations in the department of physics and mathematics of Kiev University. He passed the examinations for the master's degree at [St. Petersburg](#) (1895), becoming lecturer at Novorossysky in 1897 and professor in 1917. Besides teaching at Novorossysky, Kagan gave higher education classes for women and presented courses at a Jewish high school. He edited *Vestnik opytnoi fiziki i elementarnoi matematiki* ("Journal of Experimental Physics and Elementary Mathematics") in 1902–1917 and was a director of a large scientific publishing house, Mathesis.

Kagan's first important work was devoted to a very original and ingenious exposition of Lobachevsky's geometry. Next he considered problems of the foundations of geometry, proposing in 1902 a system of axioms and definitions considerably different from all previously suggested, and particularly different from that of Hilbert. This system was based on the notion of space as a set of points in which to every two points there corresponds a nonnegative number—distance—invariant in respect to a system of point transformations (movements) in this space; the point, the principal element from which other figures are generated, is not defined. A very complete construction of Euclid's geometry on such a basis is in the first volume of Kagan's master's thesis, defended in 1907; the second volume contains a detailed history of the doctrines of the foundations of geometry. In 1903 Kagan presented a new demonstration, remarkable in its simplicity, of Dehn's well-known theorem on equal polyhedrons (1900). Since he was interested in Einstein's theory of relativity, Kagan also began studies in tensor differential geometry which he pursued intensively in Moscow, to which he moved in 1922.

For almost ten years Kagan was in charge of the science department of the state publishing house, and for many years he supervised the department of mathematical and natural sciences of the *Great Soviet Encyclopedia*. But his principal efforts were directed to Moscow University, where he was elected professor in 1922; in 1927 he organized a seminar on vector and tensor analysis, and from 1934 he held the chair of differential geometry. At Moscow, Kagan created a large scientific school with considerable influence on the development of contemporary geometrical thought; his disciples include Y. S. Dubnov, P. K. Rashevsky, A. P. Norden, and V. V. Wagner. Kagan himself was concerned mainly with the theory of subprojective spaces, a generalization of Riemannian space of constant curvature.

Kagan also wrote studies on the history of nonEuclidean geometry and published a detailed biography of Lobachevsky. He was the general editor of the five-volume edition of Lobachevsky's complete works (1946–1951).

In 1926 Kagan was raised to the rank of honored scientist of the Russian Federation; in 1943 he was awarded the U.S.S.R. State Prize.

BIBLIOGRAPHY

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II. Secondary Literature. See A. M. Lopshitz and P. K. Rashevsky, *Benjamin Fedorovich Kagan* (Moscow, 1969); I. Z. Shtokalo, ed., *Istoria otechestvennoy matematiki* ("History of Native Mathematics"), II–III (Kiev, 1967–1968), see index; and

A. P. Youshkevitch, *Istoria matematiki U Rossii do 1917 goda* ("History of Mathematics in Russia Until 1917"; Moscow, 1968), see index.

A. P. Youshkevitch