



**SHIMSHON AVRAHAM AMITSUR (1921-1994)**  
with fellow Honorary Member Nathan Jacobson on his right

## OBITUARY

### SHIMSHON AVRAHAM AMITSUR

Shimshon Avraham Amitsur, who died on 5 September 1994, was a leading algebraist whose work in many areas of algebra had a decisive influence. He had been an honorary member of the London Mathematical Society since 1989.

Shimshon Avraham Kaplan (he later hebraicized his name to Amitsur) was born on 20 August 1921 in Jerusalem, in the old City, to Jacob and Rashke Kaplan. His father was a printer by profession, and a poet and writer by vocation (he left behind a long diary, written from boyhood in 1912 until his death in 1967). Shimshon's great-grandparents on both sides had emigrated from Russia in the 1870s and had settled in Jerusalem, earning a modest living and at the same time pursuing biblical learning.

Shimshon's talent and flair for mathematics was noticed by his secondary school teachers, who persuaded him to go to University (rather than become an accountant, as he had intended) and even obtained a stipend for him. He began his studies at the Hebrew University in Jerusalem in 1938, reading mathematics and physics, and graduated in 1941/2. He then joined the British Army (Jewish Brigade) and served for four years in the Artillery Unit, where his mathematical expertise was put to good use. There he also acquired experience as a radio operator and technician, which was to prove useful later in the defence of Mt Scopus during the War of Independence. It was at this time, in the late 1940s, that he changed his name, taking 'ami' and 'tsur' from the names of the Patriarchs of the tribes of Israel. He married Sarah, née Frankel, and they had three children (and now seven grandchildren, ranging in age from 22 to 3 years).

Returning to the Hebrew University in 1947, he received an MSc degree and the Jabotinsky Prize for research. His research in algebra, under the direction of Jacob Levitzki, led to a PhD in 1949. In 1950, Amitsur and Levitzki jointly published what has become one of the standard theorems on polynomial identities, the Amitsur-Levitzki theorem [8]: The ring of  $n \times n$  matrices over a commutative ring satisfies the standard identity of degree  $2n$ . (This was known to be the lowest possible degree, by [11].) In 1953 they shared the first Israel Prize in the Exact Sciences. In conversations with Shimshon, it was clear what an important role Levitzki had played in his professional formation. It is sad that Professor Levitzki died three years later, in 1956, and in 1974 Amitsur organized a Memorial Number of the *Israel Journal of Mathematics* in his honour ([74]; see also [38]).

Amitsur spent almost all his working life (except for overseas visiting appointments) at the Hebrew University, Jerusalem, as research assistant from 1947, instructor from 1954, lecturer from 1954, associate professor from 1956 and full professor from 1960. He was Chairman of the Mathematics Institute at the Hebrew University from 1960 to 1962.

One of Amitsur's first and lasting interests was the topic of polynomial identities in rings. The subject had received its initial impetus in 1948 when Kaplansky proved his PI-theorem [9]: A primitive algebra satisfying a polynomial identity of degree  $d$  is simple of finite dimension  $n^2$ , where  $2n \leq d$ . Building on this, Amitsur extended

his work with Levitzki by proving [13]: Any semiprime PI-ring can be embedded in a matrix ring over a commutative reduced ring. In later papers [16, 18], he generalized and strengthened these results, and put them in a more general context. As interesting by-products, he showed that (i) every integral domain satisfying a polynomial identity can be embedded in a finite-dimensional division algebra [25], (ii) every finite-dimensional division algebra can be generated by two conjugate elements  $a, u^{-1}au$  [24], (iii) every  $T$ -ideal (that is, admitting all endomorphisms) in a free algebra is primary [26]. In [59] and [66] he returned to this topic by extending the PI-theorem to general coefficient rings in an optimal way.

A significant breakthrough, which changed our perception of PI-theory, was the introduction of generalized polynomial identities (GPIs), that is, identities where the variables fail to commute not only with each other but also with the coefficients. As a first result in this field, Amitsur in [54] proved his GPI-theorem, a surprising analogue to Kaplansky's PI-theorem, this time without a bound on the dimension: A primitive ring satisfies a GPI if and only if it is isomorphic to a dense ring of linear transformations, with non-zero socle, over a skew field finite-dimensional over its centre. The proof is an ingenious but complicated induction; later, a simpler proof was found by Martindale [12] (see also Rowen [16, 17]). Amitsur went on in [58] to consider rational identities; in the non-commutative case it is by no means obvious how rational expressions should be defined, and this is not the place to go into detail. His main result was that (i) a rational identity which holds in a division algebra infinite-dimensional over an infinite centre holds universally, and (ii) a rational identity which holds in a division algebra of dimension  $n^2$  over an infinite centre, for all  $n$ , holds universally. As a consequence, he obtained a construction for the 'universal' skew field of fractions of the free algebra  $F$  (here 'universal' is to be understood as 'having all other skew fields of fractions of  $F$  as specializations'; see [4, 5]). In his later work he frequently returned to the topic of PI-rings, and also took up the topic of central polynomials, for example in [71], where he used central polynomials to give a simple proof of M. Artin's characterization of Azumaya algebras (see also [77, 78]).

I. N. Herstein in [7] made a study of the finite subgroups of skew fields, where he proved that every such subgroup of odd prime power order is cyclic, and he conjectured that this holds for any subgroup of odd order. In [28] Amitsur gave a complete solution (incidentally refuting Herstein's conjecture) by observing that such groups act without fixed points (that is, they have a representation  $\rho$  for which  $\rho(g)$  ( $g \neq 1$ ) leaves no non-zero vector fixed) and then using the classification of such groups begun by Burnside and Zassenhaus [20]. This reduces the problem to determining the existence of certain division algebras, using class-field theory. This was an astonishing *tour de force*; even more so, the fact that the problem was solved at the same time (in essentially the same way) independently by J. A. Green (who had already submitted his paper, but withdrew it when Amitsur's work appeared).

Division algebras formed another subject to which Amitsur made major contributions. It was the topic of his thesis, and at this time he proved that two central simple algebras have the same splitting fields if and only if each is similar to a power of the other in the Brauer group. In the proof, generic splitting fields play an important role. By a generic splitting field of a central simple algebra  $A$  of degree  $n$  over the base field  $k$ , one understands a field  $F(A)$  such that a field  $E$  splits  $A$  if and only if the composite  $EF(A)$  is purely transcendental of degree  $n-1$  over  $E$  (or, equivalently, there is a  $k$ -place of  $F(A)$  in  $E$ ). Such fields were studied by Witt for the

special case of quaternion algebras [\(19\)](#), and Chatelet in [\(3\)](#) made a study of algebraic varieties, the Brauer–Severi varieties, whose function fields are in effect generic splitting fields of of certain algebras. Amitsur in [\[23\]](#) was the first to define generic splitting fields for arbitrary central simple algebras, describe their properties and give methods of construction for them. Today they play an important role in the study of central simple algebras (see [\(14, 13\)](#)). In [\[29\]](#) Amitsur solved a particular case of a question raised by Jacobson [\(8\)](#), by proving that a countable-dimensional algebra over an uncountable field has a nil Jacobson radical. (He told me that he noticed this fact while lecturing on complex function theory.)

One of the key questions about division algebras concerns their representability as crossed products. In 1929 Brauer proved [\(2\)](#) that every division algebra is similar to a crossed product, and he asked whether perhaps every division algebra is isomorphic to a crossed product. A. A. Albert [\(1\)](#) showed that this was so in degree 4, and, with older results, this provided a positive answer for degrees  $n = 2, 3, 4, 6$  and 12; but the general question remained open for over 40 years, until in 1971 Amitsur was invited to contribute to a 65th birthday celebration volume for A. A. Albert. (Sadly, by the time it appeared, it was as a memorial volume.) Shimshon felt that this called for something special; he thought of the old problem of whether every central division algebra is a crossed product. And he succeeded in finding the solution: in [\[69\]](#) he constructed for any  $n$  divisible by 8 or the square of an odd prime, a division algebra of degree  $n$  that is not a crossed product. The proof is an ingenious combination of properties of generic matrix algebras and particular properties of power series rings, and it stimulated much of the recent research on division algebras.

Amitsur has been described as a ‘bare-hands mathematician’, but he managed to do a lot with his bare hands, as is shown by the many hard problems he solved. However, he also turned his hand to building theories. In a series of papers [\[14, 19, 20\]](#), he laid the foundations of a general theory of radicals in rings. Kurosh [\(10\)](#) had done the same independently, at about the same time, and it formed the basis of most subsequent treatments (see Szász [\(18\)](#)); it also had significant implications for torsion theories.

In [\[42\]](#) Amitsur introduced a complex for a field extension  $F/C$ , soon to become known as the Amitsur complex, which for Galois extensions with group  $G$  led to the cohomology of  $G$ ; he found a link with the Brauer group of  $C$  even for purely inseparable extensions. This work was generalized and simplified (with some errors corrected) by Rosenberg and Zelinsky [\(15\)](#), and it eventually became part of Čech cohomology in Grothendieck’s super-generalization of topological spaces (sites), but it took someone of Amitsur’s mathematical acumen to realize the usefulness of this complex (see also [\[50, 53\]](#)). He followed this up in joint papers with J.-P. Tignol [\[93, 94, 95\]](#), in which information on the Galois group of the minimal Galois splitting fields of universal division algebras of a given degree is obtained, leading to an evaluation of how far the universal division algebra is from being a crossed product. He also gave a treatment of derived functors in an abstract setting, in [\[49\]](#).

Amitsur used algebraic methods to good effect in other fields. Using the algebra of generating functions, he obtained results on asymptotic behaviour that led to simpler proofs of several results in number theory, including a proof of the prime number theorem ([\[39\]](#); see also [\[45, 47, 51\]](#)). His earliest work was on linear differential equations, which he viewed as linear differential operators [\[4\]](#); later, he applied these results to the study of cyclic Galois extensions of skew fields in [\[21\]](#), extending the work of Dieudonné in the quadratic case [\(6\)](#).

On a personal level, Amitsur was very approachable, and when confronted by a mathematical question, would combine his wide knowledge with some quick reflection to give a constructive reply, which would always be practical and down-to-earth. He was also very knowledgeable about biblical history, as well as modern archaeology, and it was a pleasure to follow one of his conducted tours, a pleasure he obviously shared.

He was a frequent visitor at universities in the USA and elsewhere. He was also much in demand as a speaker at conferences, and he wrote a number of illuminating survey articles [55, 65, 67, 68, 75, 80, 83, 84, 88, 90], but sadly no books. When I first met him in 1958 at the International Congress in Edinburgh, my little book on Lie groups had just appeared, and on being introduced, he said to me: 'I was sure you were an old man, because you had written a book'. But he very much kept up his research until the end. In 1969 he was awarded the Rothschild Prize for Mathematics, and he became a member of the Israel Academy of Sciences and Humanities. In 1989 our Society elected him an Honorary Member. In 1990 he received the Dr *Honoris Causa* of Ben Gurion University. He was also on the Editorial Board of numerous mathematical periodicals.

Amitsur took a keen interest in mathematical education. From 1961 to 1972 he was Director of a new experimental programme in 'New Math' in Israel, and from 1967 to 1973 he was Advisor and Writer for Instructional Television in Israel. Since 1963 he had represented the Mathematical Union of Israel at ICMI. Since 1975 he had been a member of the Committee for High School Mathematics in Israel, and since 1976 coordinator of the project of the new programme on High School Mathematics in Israel. Since 1984 he had been Director of the Education Center of the Hebrew University.

I am greatly indebted to Dr Oded Irshai, Shimshon's son-in-law, for providing me with information about the family. I should also like to thank his many friends and colleagues who have helped me in the writing of this obituary, in particular G. M. Bergman, M. P. Drazin, E. Formanek, J. Golan, A. W. Goldie, J. A. Green, I. Kaplansky, A. Mann, J. C. Robson, L. H. Rowen, J.-P. Tignol and D. Zelinsky (who kindly supplied the photograph).

### References

- ⟨1⟩. A. A. ALBERT, *Structure of algebras*, Amer. Math. Soc. Colloq. Publ. XXIV (Amer. Math. Soc., Providence, RI, 1939).
- ⟨2⟩. R. BRAUER, 'Über hyperkomplexe Systeme', *Math. Z.* 30 (1929) 79–107.
- ⟨3⟩. F. CHATELET, 'Variations sur un thème de Poincaré', *Ann. Sci. École Norm. Sup.* (3) 61 (1944) 249–300.
- ⟨4⟩. P. M. COHN, *Free rings and their relations*, London Math. Soc. Monographs 19 (Academic Press, London, 2nd edn, 1985).
- ⟨5⟩. P. M. COHN, *Skew fields, theory of general division rings*, Encyclopedia Math. Appl. 57 (Cambridge University Press, 1995).
- ⟨6⟩. J. DIEUDONNÉ, 'Les extensions quadratiques des corps non-commutatifs et leurs applications', *Acta Math.* 87 (1952) 175–242.
- ⟨7⟩. I. N. HERSTEIN, 'Finite subgroups of a division ring', *Pacific J. Math.* 3 (1953) 121–126.
- ⟨8⟩. N. JACOBSON, 'The radical and semi-simplicity for arbitrary rings', *Amer. J. Math.* 67 (1945) 300–320.
- ⟨9⟩. I. KAPLANSKY, 'Rings with a polynomial identity', *Bull. Amer. Math. Soc.* 54 (1948) 575–580.
- ⟨10⟩. A. G. KUROSH, 'Radicals of rings and algebras' (Russian), *Mat. Sb.* 33 (1953) 13–26.
- ⟨11⟩. J. LEVITZKI, 'A theorem on polynomial identities', *Proc. Amer. Math. Soc.* 1 (1950) 334–341.
- ⟨12⟩. W. S. MARTINDALE III, 'Prime rings satisfying a generalized polynomial identity', *J. Algebra* 12 (1969) 576–584.

〈13〉. V. P. PLATONOV and V. I. YANCHEVSKII, *Finite-dimensional division algebras* (Russian), Algebra 9, Itogi Nauki i Tekhniki (VINITI, Moscow, 1992; English translation Springer, 1995).

〈14〉. P. ROQUETTE, 'On the Galois cohomology of the projective linear group and its application to the construction of generic splitting fields of algebras', *Math. Ann.* 150 (1963) 411–439.

〈15〉. A. ROSENBERG and D. ZELINSKY, 'On Amitsur's complex', *Trans. Amer. Math. Soc.* 97 (1960) 327–356.

〈16〉. L. H. ROWEN, 'Generalized polynomial identities', *J. Algebra* 34 (1975) 458–480.

〈17〉. L. H. ROWEN, *Polynomial identities in ring theory* (Academic Press, New York, 1980).

〈18〉. F. SZÁSZ, *Radikale der Ringe* (VEB Deutscher Verlag d. Wiss., Berlin, 1975).

〈19〉. E. WITT, 'Über ein Gegenbeispiel zum Normensatz', *Math. Z.* 39 (1934) 462–467.

〈20〉. H. ZASSENHAUS, 'Über endliche Fastkörper', *Hamb. Abh.* 11 (1936) 187–220.

*Publications of S. A. Amitsur*

Summary of thesis submitted to the Hebrew University 1949: 'Contributions to the theory of central simple algebras'.

1. 'Applications of the theory of linear differential equations I' (Hebrew), *Riveon Lematematika* 1 (1947) 47–48.
2. 'Applications of the theory of linear differential equations II' (Hebrew), *Riveon Lematematika* 1 (1947) 79–82.
3. 'On unique factorization in rings' (Hebrew), *Riveon Lematematika* 2 (1948) 28–29.
4. 'A generalization of a theorem on linear differential equations', *Bull. Amer. Math. Soc.* 54 (1948) 937–941.
5. 'On a lemma of Kaplansky' (Hebrew, English summary), *Riveon Lematematika* 3 (1949) 47–48, 52.
6. 'La représentation d'algèbres centrales simples', *C. R. Acad. Sci. Paris* 230 (1950) 902–904.
7. 'Construction d'algèbres centrales simples sur un corps de caractéristique zéro', *C. R. Acad. Sci. Paris* 230 (1950) 1026–1028.
8. (with J. LEVITZKI) 'Minimal identities for algebras', *Proc. Amer. Math. Soc.* 1 (1950) 449–463.
9. 'Finite differential polynomials' (Hebrew), *Riveon Lematematika* 4 (1950) 1–8.
10. (with J. LEVITZKI) 'Remarks on minimal identities for algebras', *Proc. Amer. Math. Soc.* 2 (1951) 320–327.
11. 'Nil PI-rings', *Proc. Amer. Math. Soc.* 2 (1951) 538–540.
12. 'Semigroup rings' (Hebrew, English summary), *Riveon Lematematika* 5 (1951) 5–9.
13. 'An embedding of PI-rings', *Proc. Amer. Math. Soc.* 3 (1952) 3–9.
14. 'A general theory of radicals: I. Radicals in complete lattices', *Amer. J. Math.* 74 (1952) 774–786.
15. 'The problem of Kurosh–Levitzki–Jacobson' (Hebrew, English summary), *Riveon Lematematika* 5 (1951) 41–48.
16. 'The identities of PI-rings', *Proc. Amer. Math. Soc.* 4 (1953) 27–34.
17. (with A. MANY and U. OPPENHEIM) 'An electrical computer for the solution of simultaneous linear equations', *Rev. Scientific Instruments* 24 (1953) 112–116.
18. 'An identity and its applications' (Hebrew, English summary), *Riveon Lematematika* 7 (1954) 30–32.
19. 'A general theory of radicals: II. Radicals in rings and bicategories', *Amer. J. Math.* 76 (1954) 100–125.
20. 'A general theory of radicals: III. Applications', *Amer. J. Math.* 76 (1954) 126–136.
21. 'Non-commutative cyclic fields', *Duke Math. J.* 21 (1954) 87–105.
22. 'Differential polynomials and division algebras', *Ann. of Math.* (2) 59 (1954) 245–278.
23. 'Generic splitting fields of central simple algebras', *Ann. of Math.* (2) 62 (1955) 8–43.
24. 'Identities and generators of matrix rings', *Bull. Research Council Israel Sect. A* 5 (1955) 5–10.
25. 'On rings with identities', *J. London Math. Soc.* 30 (1955) 464–470.
26. 'The  $T$ -ideals of the free ring', *J. London Math. Soc.* 30 (1955) 470–475.
27. 'The radical ring generated by a single element' (Hebrew, English summary), *Riveon Lematematika* 9 (1955) 41–44.
28. 'Finite subgroups of division rings', *Trans. Amer. Math. Soc.* 80 (1955) 361–386.
29. 'Algebras over infinite fields', *Proc. Amer. Math. Soc.* 7 (1956) 35–48.
30. 'Some results on central simple algebras', *Ann. of Math.* (2) 63 (1956) 285–293.
31. 'Radicals of polynomial rings', *Canad. J. Math.* 8 (1956) 355–361.
32. 'Invariant submodules of simple rings', *Proc. Amer. Math. Soc.* 7 (1956) 987–989.
33. 'Hermite rings and the equivalence of matrices' (Hebrew, English summary), *Riveon Lematematika* 10 (1956) 41–45.
34. 'Derivations in simple rings', *Proc. London Math. Soc.* (3) 7 (1957) 87–112.
35. 'Generalization of Hilbert's Nullstellensatz', *Proc. Amer. Math. Soc.* 8 (1957) 649–656.
36. 'The radical of field extensions', *Bull. Research Council Israel Sect. F* 7 (1957) 1–10.
37. 'Countably generated division algebras over non-denumerable fields', *Bull. Research Council Israel Sect. F* 7 (1957) 39.

38. 'The scientific work of Jakob Levitzki', *Riveon Lematematika* 11 (1957) 1–6.
39. 'On arithmetic functions', *J. Analyse Math.* 5 (1958) 273–314.
40. 'Commutative linear differential operators', *Pacific J. Math.* 8 (1958) 1–10.
41. 'Rings with a pivotal monomial', *Proc. Amer. Math. Soc.* 9 (1958) 635–642.
42. 'Simple algebras and cohomology groups of arbitrary fields', *Trans. Amer. Math. Soc.* 90 (1959) 73–112.
43. 'On the semisimplicity of group algebras', *Michigan Math. J.* 6 (1959) 251–253.
44. 'Some results on arithmetic functions', *J. Math. Soc. Japan* 11 (1959) 275–279.
45. 'Convolutions of arithmetic functions' (Hebrew, English summary), *Riveon Lematematika* 13 (1959) 1–12.
46. 'Finite-dimensional central division algebras', *Proc. Amer. Math. Soc.* 11 (1960) 28–31.
47. 'Arithmetical linear transformations and abstract prime number theorems', *Canad. J. Math.* 13 (1961) 83–109; Correction, *ibid.* 21 (1969) 1–5.
48. 'Groups with representations of bounded degree II', *Illinois J. Math.* 5 (1961) 198–205.
49. 'Derived functors in abelian categories', *J. Math. Mech.* 10 (1961) 971–994.
50. 'Homology groups and double complexes for arbitrary fields', *J. Math. Soc. Japan* 14 (1962) 1–25.
51. 'On a lemma in elementary proofs of the prime number theorem', *Bull. Research Council Israel Sect. F* 10 (1962) 101–108.
52. 'Remarks on principal ideal rings', *Osaka J. Math.* 15 (1963) 59–69.
53. 'Complexes of rings', *Israel J. Math.* 2 (1964) 143–154.
54. 'Generalized polynomial identities and pivotal monomials', *Trans. Amer. Math. Soc.* 114 (1965) 210–226.
55. 'Identical relations in associative rings. Some aspects of ring theory', *CIME Conference II, Varenna (Como)* (1965) 1–48.
56. (with C. PROCESI) 'Jacobson rings and Hilbert algebras with polynomial identities', *Ann. Mat. Pura Appl.* (4) 71 (1966) 61–72.
57. 'Nil semi-groups of rings with a polynomial identity', *Nagoya Math. J.* 27 (1966) 103–111.
58. 'Rational identities and applications to algebra and geometry', *J. Algebra* 3 (1966) 304–359.
59. 'Prime rings having polynomial identities with arbitrary coefficients', *Proc. London Math. Soc.* (3) 17 (1967) 470–486.
60. 'Rings with involution', *Israel J. Math.* 6 (1968) 99–106.
61. 'Identities in rings with involutions', *Israel J. Math.* 7 (1969) 63–68.
62. 'A noncommutative Hilbert basis theorem and subrings of matrices', *Trans. Amer. Math. Soc.* 149 (1970) 133–142.
63. 'Rings of quotients and Morita contexts', *J. Algebra* 17 (1971) 273–298.
64. 'Embeddings in matrix rings', *Pacific J. Math.* 36 (1971) 21–29.
65. 'Some results on rings with polynomial identities', *Actes du Congrès International des Mathématiciens (Nice 1970)*, Vol. 1 (Gauthier-Villars, Paris, 1971) 269–272.
66. 'A note on PI-rings', *Israel J. Math.* 10 (1971) 210–211.
67. 'Nil radicals, historical notes and some new results', *Rings, modules and radicals*, Proc. Colloq. Keszthely 1971, Vol. 6 (North-Holland, Amsterdam, 1973) 47–65.
68. 'On rings of quotients', *Convegno sulle Algebre Associative INDAM Roma 1970*, Sympos. Math. VIII (Academic Press, London, 1972) 149–164.
69. 'On central division algebras', *Israel J. Math.* 12 (1972) 408–420.
70. 'On universal embeddings in matrix rings', *J. Math. Soc. Japan* 25 (1973) 322–328.
71. 'Polynomial identities and Azumaya algebras', *J. Algebra* 27 (1973) 117–125.
72. 'On supernilpotent radicals', *Estudos Mat. Lisboa* (1974) 51–56.
73. 'The generic division rings', *Israel J. Math.* 17 (1974) 241–247.
74. 'Jacob Levitzki, 1904–1956', *Israel J. Math.* 19 (1974) 1–2.
75. 'Polynomial identities', *Israel J. Math.* 19 (1974) 183–199.
76. 'Central embeddings in semisimple rings', *Pacific J. Math.* 56 (1975) 1–6.
77. 'Identities and linear dependence', *Israel J. Math.* 22 (1975) 127–137.
78. 'On a central identity of matrix rings', *J. London Math. Soc.* (2) 14 (1976) 1–6.
79. (with L. W. SMALL) 'Prime PI-rings', *Bull. Amer. Math. Soc.* 83 (1977) 249–251.
80. 'Alternating identities', *Ring theory*, Proc. Conf. Ohio Univ., Athens Ohio, 1976, Lecture Notes in Pure and Appl. Math. 25 (Dekker, New York, 1977) 1–4.
81. (with D. J. SALTMAN) 'Generic abelian crossed products and  $p$ -algebras', *J. Algebra* 51 (1978) 76–87.
82. (with L. W. SMALL) 'Polynomials over division rings', *Israel J. Math.* 31 (1978) 353–358.
83. 'Polynomial identities and division algebras', *Generic division algebras*, Arbeitsgemeinschaft Algebra: Schiefkörper, Oberwolfach (1978) 1–8.
84. 'The polynomial identities of associative rings', *Conference on Noetherian rings and rings with polynomial identities*, Durham (1979) 1–38.
85. (with L. H. ROWEN and J.-P. TIGNOL) 'Division algebras of degree 4 and 8 with involution', *Bull. Amer. Math. Soc. (N.S.)* 1 (1979) 691–693; *Israel J. Math.* 33 (1979) 133–148.

86. 'On the characteristic polynomial of a sum of matrices', *Linear and Multilinear Algebra* 8 (1980) 177–182.
87. (with L. W. SMALL) 'Prime ideals in PI-rings', *J. Algebra* 62 (1980) 358–383.
88. 'Generic splitting fields', *Brauer groups in ring theory and algebraic geometry*, Proc. Antwerp 1981, Lecture Notes in Math. 917 (Springer, Berlin, 1982) 1–24.
89. 'Extensions of derivations to central simple algebras', *Comm. Algebra* 10 (1982) 797–803.
90. 'Division algebras. A survey', *Algebraists' homage: Papers in ring theory and related topics*, New Haven, Conn. 1981, Contemp. Math. 13 (Amer. Math. Soc., Providence, RI, 1982) 3–26.
91. (with A. REGEV) 'PI-algebras and their cocharacters', *J. Algebra* 78 (1982) 248–254.
92. 'The sequence of co-dimensions of PI-algebras', *Israel J. Math.* 47 (1984) 1–22.
93. (with J.-P. TIGNOL) 'Kummer subfields of Malcev–Neumann algebras', *Israel J. Math.* 50 (1985) 114–144.
94. (with J.-P. TIGNOL) 'Symplectic modules', *Israel J. Math.* 54 (1986) 266–290.
95. (with J.-P. TIGNOL) 'Totally ramified splitting fields of central simple algebras over henselian fields', *Inst. Math. Univ. Catholique de Louvain-La-Neuve* 36 (1983) iv1–iv9; *J. Algebra* 98 (1986) 95–101.
96. 'An example in central division algebras', *Perspectives in ring theory*, NATO Adv. Study Inst. 233 (1987) 85–92.
97. (with L. W. SMALL) 'Finite representation of PI-algebras', *J. Algebra* 133 (1990) 244–248.
98. (with L. W. SMALL) 'GK-dimensions of corners and ideals', *Israel J. Math.* 69 (1990) 152–160.
99. 'Some highlights in the history of finite-dimensional central division algebras', *Ring theory 1989 in honor of S. A. Amitsur* (Ramat Gan and Jerusalem 1988/9) Israel Math. Conf. Proc. 1 (Weizmann Sci. Press, Jerusalem, 1989) 404–430.
100. 'Galois splitting fields of a universal division algebra', *J. Algebra* 143 (1991) 236–245.
101. 'Generic structures and division algebras', *Sém. Math. Rapport* 171 (Univ. Catholique de Louvain, 1990) 1–12.
102. (with L. W. SMALL) 'Affine algebras with polynomial identities', *Rend. Circ. Mat. Palermo (2) Suppl.* 31 (1993) 9–43.
103. (with L. W. SMALL) 'Finite-dimensional representation of PI-algebras II', *J. Algebra* 174 (1995) 848–855.
104. (with L. H. ROWEN) 'Elements of reduced trace 0', *Israel J. Math.* 87 (1994) 161–179.
105. 'Contributions of PI-algebras to Azumaya algebras', *Rings, extensions and cohomology* (Evanston, IL, 1993), Lecture Notes in Pure and Appl. Math. 159 (Dekker, New York, 1994) 9–17.
106. (with J. C. ROBSON and G. AGNARSSON) 'Recognition of matrix rings II', to appear.

Department of Mathematics  
 University College London  
 Gower Street  
 London WC1E 6BT

P. M. COHN